

$$\left\{ \begin{array}{l}
\sigma_{pp} = 9B \ln^2 \left( \frac{s}{s_0} \right) + Y_1^{pp} s^{-\eta_1} - Y_2^{pp} s^{-\eta_2}, \\
\sigma_{\bar{p}p} = 9B \ln^2 \left( \frac{s}{s_0} \right) + Y_1^{pp} s^{-\eta_1} + Y_2^{pp} s^{-\eta_2}, \\
\sigma_{\pi^+p} = 6\lambda_m B \ln^2 \left( \frac{s}{s_0} \right) + Y_1^{\pi p} s^{-\eta_1} - Y_2^{\pi p} s^{-\eta_2}, \\
\sigma_{\pi^-p} = 6\lambda_m B \ln^2 \left( \frac{s}{s_0} \right) + Y_1^{\pi p} s^{-\eta_1} + Y_2^{\pi p} s^{-\eta_2}, \\
\sigma_{K^+p} = 3\lambda_m(1 + \lambda_s) B \ln^2 \left( \frac{s}{s_0} \right) + Y_1^{Kp} s^{-\eta_1} - Y_2^{Kp} s^{-\eta_2}, \\
\sigma_{K^-p} = 3\lambda_m(1 + \lambda_s) B \ln^2 \left( \frac{s}{s_0} \right) + Y_1^{Kp} s^{-\eta_1} + Y_2^{Kp} s^{-\eta_2}, \\
\sigma_{\gamma p} = 6\lambda_m \delta B \ln^2 \left( \frac{s}{s_0} \right) + Y_1^{\gamma p} s^{-\eta_1}, \\
\sigma_{\gamma\gamma} = 4\lambda_m^2 \delta^2 B \ln^2 \left( \frac{s}{s_0} \right) + Y_1^{\gamma\gamma} s^{-\eta_1}, \\
\sigma_{\Sigma^-p} = (6 + 3\lambda_s) B \ln^2 \left( \frac{s}{s_0} \right) + Y_1^{\Sigma p} s^{-\eta_1} - Y_2^{\Sigma p} s^{-\eta_2}. \quad \blacksquare \\
\rho_{pp}\sigma_{pp} = 9\pi B \ln \left( \frac{s}{s_0} \right) - \frac{Y_1^{pp} s^{-\eta_1}}{\tan \left[ \frac{1 - \eta_1}{2} \pi \right]} - \frac{Y_2^{pp} s^{-\eta_2}}{\cot \left[ \frac{1 - \eta_2}{2} \pi \right]}, \\
\rho_{\bar{p}p}\sigma_{\bar{p}p} = 9\pi B \ln \left( \frac{s}{s_0} \right) - \frac{Y_1^{pp} s^{-\eta_1}}{\tan \left[ \frac{1 - \eta_1}{2} \pi \right]} + \frac{Y_2^{pp} s^{-\eta_2}}{\cot \left[ \frac{1 - \eta_2}{2} \pi \right]}, \\
\rho_{\pi^+p}\sigma_{\pi^+p} = 6\pi \lambda_m B \ln \left( \frac{s}{s_0} \right) - \frac{Y_1^{\pi p} s^{-\eta_1}}{\tan \left[ \frac{1 - \eta_1}{2} \pi \right]} - \frac{Y_2^{\pi p} s^{-\eta_2}}{\cot \left[ \frac{1 - \eta_2}{2} \pi \right]}, \\
\rho_{\pi^-p}\sigma_{\pi^-p} = 6\pi \lambda_m B \ln \left( \frac{s}{s_0} \right) - \frac{Y_1^{\pi p} s^{-\eta_1}}{\tan \left[ \frac{1 - \eta_1}{2} \pi \right]} + \frac{Y_2^{\pi p} s^{-\eta_2}}{\cot \left[ \frac{1 - \eta_2}{2} \pi \right]}, \\
\rho_{K^+p}\sigma_{K^+p} = 3\pi \lambda_m(1 + \lambda_s) B \ln \left( \frac{s}{s_0} \right) - \frac{Y_1^{Kp} s^{-\eta_1}}{\tan \left[ \frac{1 - \eta_1}{2} \pi \right]} - \frac{Y_2^{Kp} s^{-\eta_2}}{\cot \left[ \frac{1 - \eta_2}{2} \pi \right]}, \\
\rho_{K^-p}\sigma_{K^-p} = 3\pi \lambda_m(1 + \lambda_s) B \ln \left( \frac{s}{s_0} \right) - \frac{Y_1^{Kp} s^{-\eta_1}}{\tan \left[ \frac{1 - \eta_1}{2} \pi \right]} + \frac{Y_2^{Kp} s^{-\eta_2}}{\cot \left[ \frac{1 - \eta_2}{2} \pi \right]},
\end{array} \right.$$

Variable  $s$  is in the units  $[GeV^2]$ . The additional scale  $s_1 = 1 [GeV^2]$  in terms with  $(s/s_1)^{-\eta_{1,2}}$  is omitted for brevity.

Adjustable parameters naming. In total 17 parameters used:

$$\begin{aligned} \eta_1, \eta_2, \delta, \lambda_m, \lambda_s & - \text{dimensionless} \\ s_0 & - [\text{GeV}^2] \\ B, Y_{1,2}^{pp}, Y_{1,2}^{\pi p}, Y_{1,2}^{Kp}, Y_{1,2}^{\Sigma p}, Y_1^{\gamma p}, Y_1^{\gamma\gamma} & - [\text{mb}] \end{aligned}$$

Scan-fits summary. 2000 database. Without cosmic data points.

$E_{\text{cm}}^{\text{min}}$ [GeV]	3	4	5	6	7	8	9	10
$N_{\text{dof}}$ : $\rho$ excluded	709	564	490	417	352	314	268	213
$N_{\text{dof}}$ : $\rho$ included	887	725	631	552	481	436	380	312
$\chi^2/\text{dof}$ : $\rho$ excluded	1.33	1.06	0.88	0.85	0.88	0.88	0.90	0.89
$\chi^2/\text{dof}$ : $\rho$ included	1.68	1.22	1.04	1.04	1.05	1.01	0.97	0.97

Details of the fit to the data in the whole domain of applicability

	$\sqrt{s}$ of the starting point in [GeV]	Number of data points	$\chi^2/\text{dof}$	=	<b>0.97</b>
			CL[%]	=	64.2
Breakdown of the CS data sample			Name of value	Numerical value	Error value
$pp$ :	9.02958	74	$\eta_1$	0.27261187	0.01145315
$\bar{p}p$ :	9.02958	35	$\eta_2$	0.5552468	0.011697771
$\pi^+p$ :	9.23822	24	$\lambda_s$	0.8168957	0.009981307
$\pi^-p$ :	9.23822	49	$\lambda_m$	0.99178998	0.0049437527
$K^+p$ :	9.2506	22	$\delta$	0.0049039875	0.000059129061
$K^-p$ :	9.2506	28	$B$	0.016076625	0.00084766039
$\Sigma^-p$ :	11.922	8	$s_0$	0.00044830086	0.00024455797
$\gamma p$ :	9.12473	25	$Y_{pp1}$	67.01912	1.110379
$\gamma\gamma$ :	9.	20	$Y_{pp2}$	35.528122	2.1696148
Breakdown of the $\rho$ data sample			$Y_{\pi p1}$	32.044131	0.39094229
$pp$ :	9.02958	59	$Y_{\pi p2}$	7.3987287	0.48735937
$\bar{p}p$ :	11.5382	11	$Y_{Kp1}$	21.309284	0.42014885
$\pi^+p$ :	9.94262	7	$Y_{Kp2}$	14.338892	0.86291144
$\pi^-p$ :	9.28583	23	$Y_{\gamma p1}$	0.15235874	0.0039571782
$K^+p$ :	9.9541	7	$Y_{\gamma\gamma1}$	0.00020571091	0.000053026337
$K^-p$ :	11.5102	5	$Y_{\Sigma p1}$	57.37743	5.3027903
			$Y_{\Sigma p2}$	57.69251	22.760787

Model quality indicators:

	$A^M$	$C_1^M$	$C_2^M$	$U^M$	$R_1^M$	$R_2^M$	$S_1^M$	$S_2^M$
RRL2 <sup>qc</sup> (17)	1.726	64.2	64.2	11.23	22.06	0.941	1.318	2.503

Repository:

computer - NPT1

directory - d:\MathemD\Kolja\Evela\Gauron\((RR)L2qc(17)

Appendix RRL2<sub>qc</sub>(17) (N<sup>o</sup>12)  $\chi^2/\text{NoP}$  by data samples

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	CS data								
Reaction	$pp$	$\bar{p}p$	$\pi^+p$	$\pi^-p$	$K^+p$	$K^-p$	$\Sigma^-p$	$\gamma p$	$\gamma\gamma$
$\chi^2/\text{NoP}$	1.03	1.21	0.47	1.03	0.45	0.75	0.43	0.68	0.65

	$\rho$ data					
Reaction	$pp$	$\bar{p}p$	$\pi^+p$	$\pi^-p$	$K^+p$	$K^-p$
$\chi^2/\text{NoP}$	1.27	0.42	2.0	0.75	0.69	1.88

# Correlation matrix

## RRL2<sup>qc</sup>(17) (N=12)

### Appendix

	$\eta_1$	$\eta_2$	$\lambda_s$	$\lambda_m$	$\delta$	$B$	$s_0$	$Y_{pp1}$	$Y_{pp2}$	$Y_{\pi p1}$	$Y_{\pi p2}$	$Y_{Kp1}$	$Y_{Kp2}$	$Y_{\gamma p1}$	$Y_{\gamma p2}$	$Y_{\Sigma p1}$	$Y_{\Sigma p2}$
$\eta_1$	100	23.2	-66.5	-71.6	-2.33	<b>-90.8</b>	<b>-93.8</b>	74.6	21.8	18	23.8	-41.5	22.5	4.6	-21.9	14.7	5.04
$\eta_2$	23.2	100	-19.8	17.8	-4.76	-9.92	-11.1	46.7	<b>98.5</b>	26.4	<b>90.7</b>	12.8	<b>96.3</b>	16.3	-4.82	5.26	11.7
$\lambda_s$	-66.5	-19.8	100	26.5	9.91	60.4	62.3	-50.3	-18.8	3.88	-22.3	-1.57	-16.8	-3.22	14.6	-20.4	-11.2
$\lambda_m$	-71.6	17.8	26.5	100	-9.78	78.3	79.2	-24.5	18.8	-0.33	16.6	56.1	17	13.7	16.7	-0.297	4.99
$\delta$	-2.33	-4.76	9.91	-9.78	100	0.887	1.08	-4.32	-4.7	4.12	-5.51	-1.42	-4.58	-86.3	-62.5	-2.38	-1.79
$B$	<b>-90.8</b>	-9.92	60.4	78.3	0.887	100	<b>99.6</b>	-41.8	-8.46	21.3	-11.8	69.6	-9.78	15.3	22.8	-7.75	-2.48
$s_0$	<b>-93.8</b>	-11.1	62.3	79.2	1.08	<b>99.6</b>	100	-48	-9.65	14.2	-12.9	65.4	-10.9	11.9	22.9	-9.01	-2.73
$Y_{pp1}$	74.6	46.7	-50.3	-24.5	-4.32	-41.8	-48	100	46.6	70.1	43.8	17.6	44.9	33.6	-12.6	20.6	9.18
$Y_{pp2}$	21.8	<b>98.5</b>	-18.8	18.8	-4.7	-8.46	-9.65	46.6	100	26.7	89.3	13.7	<b>94.9</b>	16.5	-4.48	5.21	11.6
$Y_{\pi p1}$	18	26.4	3.88	-0.33	4.12	21.3	14.2	70.1	26.7	100	19.2	61.4	25.2	43	2.35	12.2	3.46
$Y_{\pi p2}$	23.8	<b>90.7</b>	-22.3	16.6	-5.51	-11.8	-12.9	43.8	89.3	19.2	100	9.85	87.3	14.5	-5.01	5.56	11
$Y_{Kp1}$	-41.5	12.8	-1.57	56.1	-1.42	69.6	65.4	17.6	13.7	61.4	9.85	100	9.68	34	14.3	10.1	6.06
$Y_{Kp2}$	22.5	<b>96.3</b>	-16.8	17	-4.58	-9.78	-10.9	44.9	<b>94.9</b>	25.2	87.3	9.68	100	15.6	-4.69	4.59	11
$Y_{\gamma p1}$	4.6	16.3	-3.22	13.7	-86.3	15.3	11.9	33.6	16.5	43	14.5	34	15.6	100	57.7	7.23	3.1
$Y_{\gamma p2}$	-21.9	-4.82	14.6	16.7	-62.5	22.8	22.9	-12.6	-4.48	2.35	-5.01	14.3	-4.69	57.7	100	-2.44	-1.05
$Y_{\Sigma p1}$	14.7	5.26	-20.4	-0.297	-2.38	-7.75	-9.01	20.6	5.21	12.2	5.56	10.1	4.59	7.23	-2.44	100	<b>98</b>
$Y_{\Sigma p2}$	5.04	11.7	-11.2	4.99	-1.79	-2.48	-2.73	9.18	11.6	3.46	11	6.06	11	3.1	-1.05	<b>98</b>	100

# Appendix RRL2<sup>qc</sup>(17) (N=12) Parameters evolution

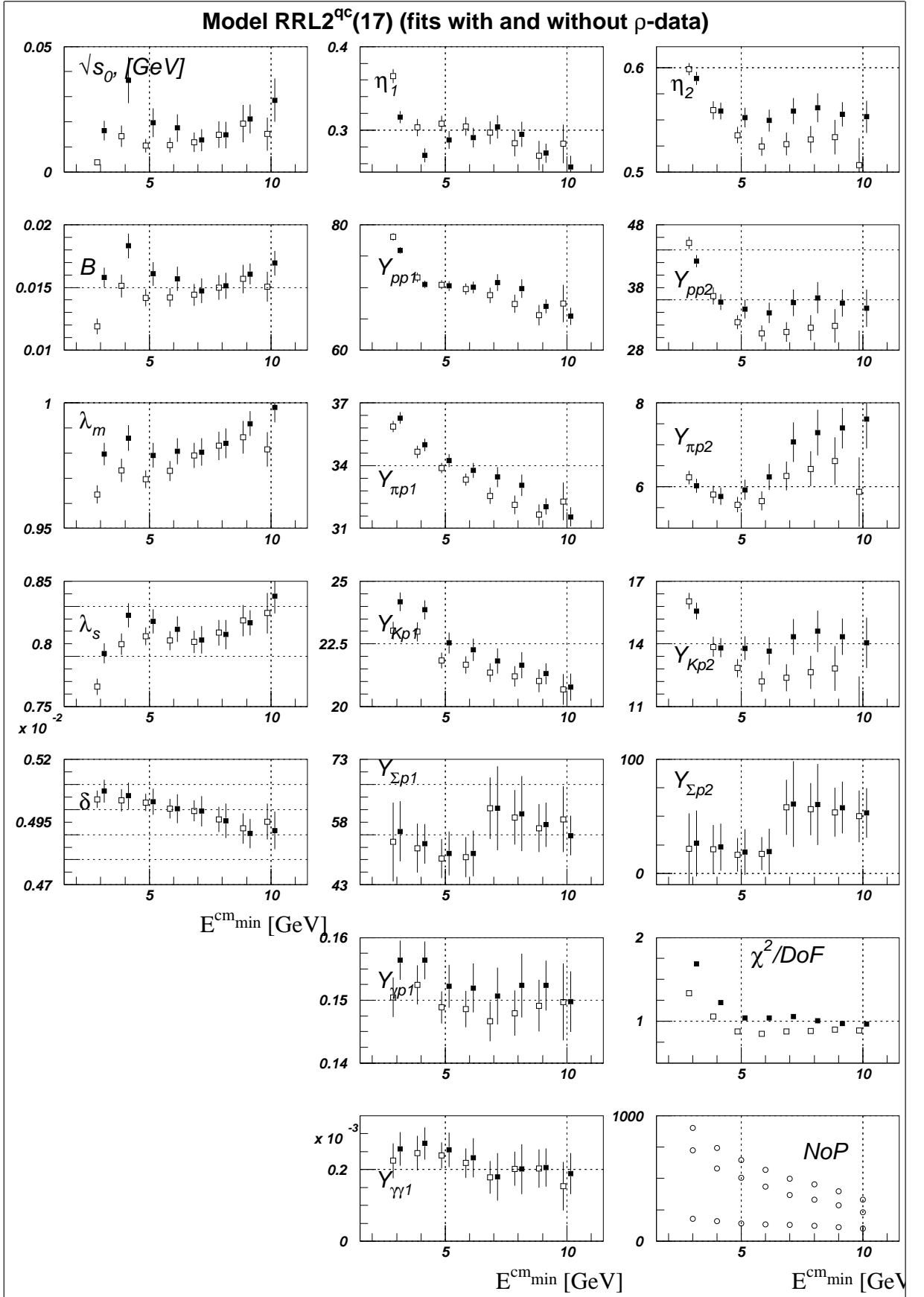


Figure 22: Bold (empty) symbol marks fits with (without)  $\rho$  data and are shifted to the right (left) in energy slightly for the cleareness

