

$$\left\{ \begin{array}{l}
\sigma_{pp} = Z_{pp} + B_{pp} \ln s + Y_1^{pp} s^{-\eta_1} - Y_2^{pp} s^{-\eta_2}, \\
\sigma_{\bar{p}p} = Z_{pp} + B_{pp} \ln s + Y_1^{pp} s^{-\eta_1} + Y_2^{pp} s^{-\eta_2}, \\
\sigma_{\pi^+p} = Z_{\pi p} + B_{\pi p} \ln s + Y_1^{\pi p} s^{-\eta_1} - Y_2^{\pi p} s^{-\eta_2}, \\
\sigma_{\pi^-p} = Z_{\pi p} + B_{\pi p} \ln s + Y_1^{\pi p} s^{-\eta_1} + Y_2^{\pi p} s^{-\eta_2}, \\
\sigma_{K^+p} = Z_{Kp} + B_{Kp} \ln s + Y_1^{Kp} s^{-\eta_1} - Y_2^{Kp} s^{-\eta_2}, \\
\sigma_{K^-p} = Z_{Kp} + B_{Kp} \ln s + Y_1^{Kp} s^{-\eta_1} + Y_2^{Kp} s^{-\eta_2}, \\
\sigma_{\gamma p} = \delta (Z_{pp} + B_{pp} \ln s) + Y_1^{\gamma p} s^{-\eta_1}, \\
\sigma_{\gamma\gamma} = \delta^2 (Z_{pp} + B_{pp} \ln s) + Y_1^{\gamma\gamma} s^{-\eta_1}, \\
\sigma_{\Sigma^-p} = Z_{\Sigma p} + B_{\Sigma p} \ln s + Y_1^{\Sigma p} s^{-\eta_1} - Y_2^{\Sigma p} s^{-\eta_2}. \quad \blacksquare \\
\rho_{pp}\sigma_{pp} = \frac{\pi B_{pp}}{2} - \frac{Y_1^{pp} s^{-\eta_1}}{\tan \left[ \frac{1-\eta_1}{2} \pi \right]} - \frac{Y_2^{pp} s^{-\eta_2}}{\cot \left[ \frac{1-\eta_2}{2} \pi \right]}, \\
\rho_{\bar{p}p}\sigma_{\bar{p}p} = \frac{\pi B_{pp}}{2} - \frac{Y_1^{pp} s^{-\eta_1}}{\tan \left[ \frac{1-\eta_1}{2} \pi \right]} + \frac{Y_2^{pp} s^{-\eta_2}}{\cot \left[ \frac{1-\eta_2}{2} \pi \right]}, \\
\rho_{\pi^+p}\sigma_{\pi^+p} = \frac{\pi B_{\pi p}}{2} - \frac{Y_1^{\pi p} s^{-\eta_1}}{\tan \left[ \frac{1-\eta_1}{2} \pi \right]} - \frac{Y_2^{\pi p} s^{-\eta_2}}{\cot \left[ \frac{1-\eta_2}{2} \pi \right]}, \\
\rho_{\pi^-p}\sigma_{\pi^-p} = \frac{\pi B_{\pi p}}{2} - \frac{Y_1^{\pi p} s^{-\eta_1}}{\tan \left[ \frac{1-\eta_1}{2} \pi \right]} + \frac{Y_2^{\pi p} s^{-\eta_2}}{\cot \left[ \frac{1-\eta_2}{2} \pi \right]}, \\
\rho_{K^+p}\sigma_{K^+p} = \frac{\pi B_{Kp}}{2} - \frac{Y_1^{Kp} s^{-\eta_1}}{\tan \left[ \frac{1-\eta_1}{2} \pi \right]} - \frac{Y_2^{Kp} s^{-\eta_2}}{\cot \left[ \frac{1-\eta_2}{2} \pi \right]}, \\
\rho_{K^-p}\sigma_{K^-p} = \frac{\pi B_{Kp}}{2} - \frac{Y_1^{Kp} s^{-\eta_1}}{\tan \left[ \frac{1-\eta_1}{2} \pi \right]} + \frac{Y_2^{Kp} s^{-\eta_2}}{\cot \left[ \frac{1-\eta_2}{2} \pi \right]},
\end{array} \right.$$

Variable  $s$  is in the units  $[GeV^2]$ . The additional scale  $s_1 = 1 [GeV^2]$  in terms with  $(s/s_1)^{-\eta_{1,2}}$  is omitted for brevity.

Adjustable parameters naming. In total 21 parameters used:

$$\begin{aligned} \eta_1, \eta_2, \delta & - \text{dimensionless} \\ \mathbf{Z}_{pp}, \mathbf{Z}_{\pi p}, \mathbf{Z}_{Kp}, \mathbf{Z}_{\Sigma p}, \mathbf{B}_{pp}, \mathbf{B}_{\pi p}, \mathbf{B}_{Kp}, \mathbf{B}_{\Sigma p} & - [\text{mb}] \\ \mathbf{Y}_{1,2}^{pp}, \mathbf{Y}_{1,2}^{\pi p}, \mathbf{Y}_{1,2}^{Kp}, \mathbf{Y}_{1,2}^{\Sigma p}, \mathbf{Y}_1^{\gamma p}, \mathbf{Y}_1^{\gamma\gamma} & - [\text{mb}] \end{aligned}$$

Scan-fits summary. 2000 database. Without cosmic data points.

$E_{\text{cm}}^{\text{min}}$ [GeV]	3	4	5	6	7	8	9	10
$N_{\text{dof}}$ : $\rho$ excluded	705	560	486	413	348	310	264	209
$N_{\text{dof}}$ : $\rho$ included	883	721	627	548	477	432	376	308
$\chi^2/\text{dof}$ : $\rho$ excluded	1.33	0.98	0.85	0.83	0.87	0.87	0.84	0.74
$\chi^2/\text{dof}$ : $\rho$ included	1.63	1.11	0.98	0.98	0.99	0.94	0.93	0.91

Details of the fit to the data in the whole domain of applicability

			$\chi^2/\text{dof}$	=	<b>0.98</b>	
			CL[%]	=	66.59	
	$\sqrt{s}$ of the starting point in [GeV]	Number of data points	Name of value	Numerical value	Error value	
Breakdown of the CS data sample			$\eta_1$	0.20804983	0.0081843967	
	$pp$ :	5.00963	112	$\eta_2$	0.53637805	0.0063821539
	$\bar{p}p$ :	5.1569	59	$\delta$	0.0034571382	0.000041246466
	$\pi^+p$ :	5.21275	50	$B_{pp}$	6.5817218	0.23374123
	$\pi^-p$ :	5.02954	106	$B_{\pi p}$	4.9677831	0.21128001
	$K^+p$ :	5.12707	40	$B_{Kp}$	4.0083088	0.20222005
	$K^-p$ :	5.10875	63	$B_{\Sigma p}$	3.6491645	9.717062
	$\Sigma^-p$ :	6.12189	9	$Y_{pp1}$	103.61068	3.0863341
	$\gamma p$ :	5.01008	38	$Y_{pp2}$	32.036043	0.94003067
	$\gamma\gamma$ :	5.	30	$Y_{\pi p1}$	65.779961	2.7899416
Breakdown of the $\rho$ data sample			$Y_{\pi p2}$	5.6445108	0.15799338	
	$pp$ :	5.30542	74	$Y_{Kp1}$	45.237665	2.66838
	$\bar{p}p$ :	11.5382	11	$Y_{Kp2}$	12.937264	0.37044689
	$\pi^+p$ :	8.98072	8	$Y_{\Sigma p1}$	0.012899879	232.50648
	$\pi^-p$ :	7.56285	30	$Y_{\Sigma p2}$	-76.574871	191.63066
	$K^+p$ :	5.21771	10	$Y_{\gamma p1}$	0.28513947	0.013159549
	$K^-p$ :	5.23565	8	$Y_{\gamma\gamma1}$	0.00074682565	0.000055617978
				$Z_{pp}$	-28.963728	3.7085676
				$Z_{\pi p}$	-24.447934	2.942881
				$Z_{Kp}$	-16.541522	2.4614956
				$Z_{\Sigma p}$	9.6315719	117.58049

Model quality indicators:

	$A^M$	$C_1^M$	$C_2^M$	$U^M$	$R_1^M$	$R_2^M$	$S_1^M$	$S_2^M$
RRPL(21)	1.607	66.59	82.16	26.29	29.45	0.752	0.210	1.135

Repository:

computer - NPT1

directory - d:\MathemD\Kolja\Evela\Gauron\ (RR)PL(21)

## Appendix RRPL(21) (N<sup>o</sup>19) $\chi^2/\text{NoP}$ by data samples

	CS data								
Reaction	$pp$	$\bar{p}p$	$\pi^+p$	$\pi^-p$	$K^+p$	$K^-p$	$\Sigma^-p$	$\gamma p$	$\gamma\gamma$
$\chi^2/\text{NoP}$	0.87	1.01	0.78	0.89	0.72	0.62	0.38	0.75	0.95

	$\rho$ data					
Reaction	$pp$	$\bar{p}p$	$\pi^+p$	$\pi^-p$	$K^+p$	$K^-p$
$\chi^2/\text{NoP}$	1.57	0.47	1.59	1.27	1.11	1.24

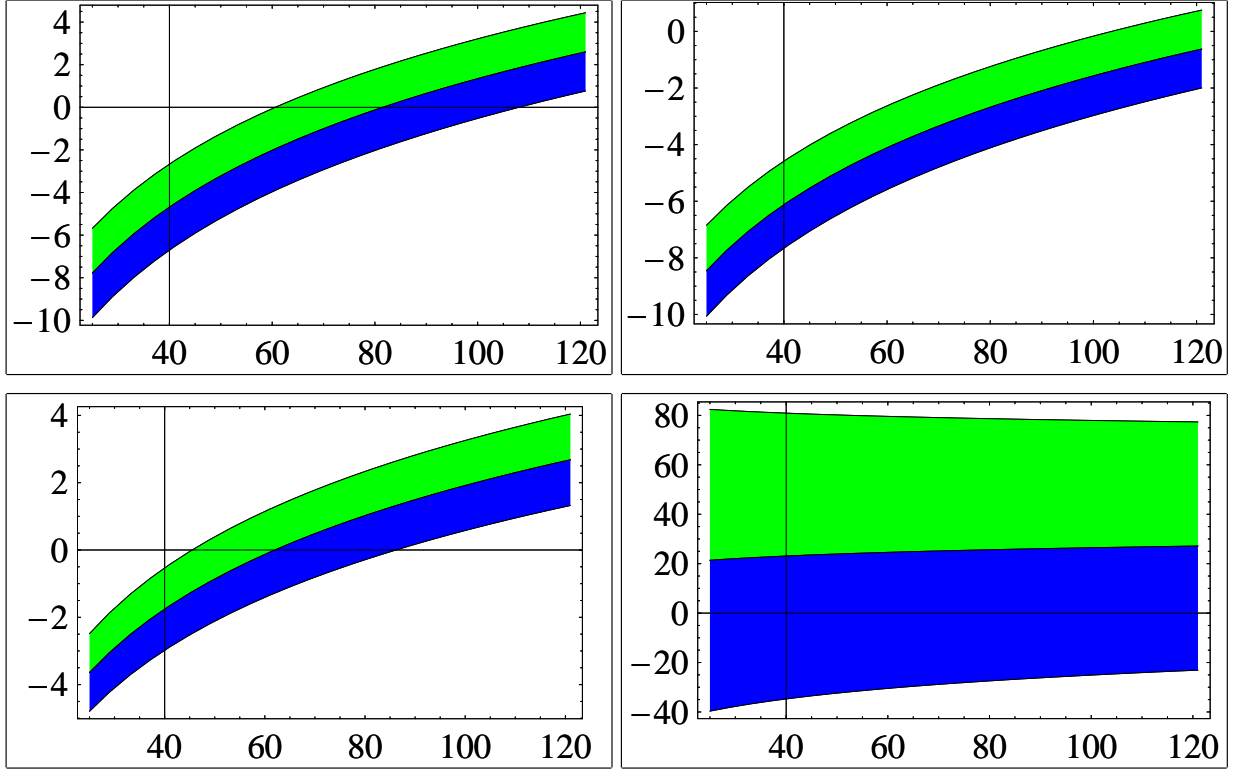


Figure 18: Pomeron contribution for  $pp$ ,  $\pi^+p$ ,  $K^+p$  and  $\Sigma^-p$ , [mb] (Axis  $X - s$  [GeV<sup>2</sup>])

	$\eta_1$	$\eta_2$	$\delta$	$B_{pp}$	$B_{\pi p}$	$B_{Kp}$	$B_{\Sigma p}$	$Y_{pp1}$	$Y_{pp2}$	$Y_{\pi p1}$	$Y_{\pi p2}$	$Y_{Kp1}$	$Y_{Kp2}$	$Y_{\Sigma p1}$	$Y_{\Sigma p2}$	$Y_{\gamma p1}$	$Y_{\gamma p2}$	$Z_{pp}$	$Z_{\pi p}$	$Z_{Kp}$	$Z_{\Sigma p}$
$\eta_1$	100	22.8	-59.5	<b>-96.2</b>	<b>-91.6</b>	-69.8	-4.07	<b>-94.5</b>	24	<b>-92.2</b>	22.6	-69.8	21.6	-4	4.06	<b>-96.4</b>	<b>-90.9</b>	<b>98.3</b>	<b>96.1</b>	82	4.05
$\eta_2$	22.8	100	-1.95	-13.7	-22.2	-14.9	0.3	-8.38	<b>97.5</b>	-22.5	88.3	-14.8	<b>94.5</b>	0.65	-0.3	-11.7	-13.1	15.9	22.9	17.8	-0.4
$\delta$	-59.5	-1.95	100	60.6	54.3	41.6	2.57	61.1	-1.72	54.6	-3.28	41.7	-1.93	2.57	-2.57	60.5	51.2	-61	-57	-48.9	-2.57
$B_{pp}$	<b>-96.2</b>	-13.7	60.6	100	88	67.2	4.02	<b>99.6</b>	-13.8	88.6	-14.6	67.3	-13.1	3.99	-4.02	<b>99.8</b>	<b>92.8</b>	<b>-99.6</b>	<b>-92.4</b>	-79	-4.02
$B_{\pi p}$	<b>-91.6</b>	-22.2	54.3	88	100	63.9	3.71	86.4	-23.2	<b>99.9</b>	-19.5	64	-21.1	3.65	-3.71	88.2	83.2	<b>-90</b>	<b>-99.1</b>	-75.1	-3.7
$B_{Kp}$	-69.8	-14.9	41.6	67.2	63.9	100	2.85	66.1	-15.8	64.3	-14.9	<b>99.8</b>	-11.3	2.81	-2.85	67.4	63.5	-68.7	-67.1	<b>-98.2</b>	-2.84
$B_{\Sigma p}$	-4.07	0.3	2.57	4.02	3.71	2.85	100	4.02	0.261	3.73	0.197	2.85	0.323	<b>99.8</b>	<b>-98.9</b>	4.06	3.8	-4.08	-3.9	-3.35	-1.00
$Y_{pp1}$	<b>-94.5</b>	-8.38	61.1	<b>99.6</b>	86.4	66.1	4.02	100	-7.86	86.9	-9.86	66.1	-8.05	4	-4.01	<b>99.7</b>	<b>92.4</b>	<b>-98.9</b>	<b>-90.7</b>	-77.6	-4.02
$Y_{pp2}$	24	<b>97.5</b>	-1.72	-13.8	-23.2	-15.8	0.261	-7.86	100	-23.6	86.2	-15.7	<b>92.1</b>	0.6	-0.2	-11.7	-13.4	16.3	24	18.8	-0.332
$Y_{\pi p1}$	<b>-92.2</b>	-22.5	54.6	88.6	<b>99.9</b>	64.3	3.73	86.9	-23.6	100	-20.1	64.4	-21.4	3.67	-3.73	88.7	83.7	<b>-90.5</b>	<b>-99.3</b>	-75.6	-3.72
$Y_{\pi p2}$	22.6	88.3	-3.28	-14.6	-19.5	-14.9	0.197	-9.86	86.2	-20.1	100	-14.8	83.5	0.463	-0.2	-12.8	-13.9	16.5	21	17.8	-0.262
$Y_{Kp1}$	-69.8	-14.8	41.7	67.3	64	<b>99.8</b>	2.85	66.1	-15.7	64.4	-14.8	100	-11.5	2.82	-2.85	67.5	63.6	-68.7	-67.1	<b>-98.2</b>	-2.85
$Y_{Kp2}$	21.6	<b>94.5</b>	-1.93	-13.1	-21.1	-11.3	0.323	-8.05	<b>92.1</b>	-21.4	83.5	-11.5	100	0.608	-0.3	-11.2	-12.5	15.1	21.8	14.8	-0.392
$Y_{\Sigma p1}$	-4	0.65	2.57	3.99	3.65	2.81	<b>99.8</b>	4	0.6	3.67	0.463	2.82	0.608	100	<b>-99.5</b>	4.03	3.76	-4.04	-3.83	-3.3	<b>-99.9</b>
$Y_{\Sigma p2}$	4.06	-0.3	-2.57	-4.02	-3.71	-2.85	<b>-98.9</b>	-4.01	-0.2	-3.73	-0.2	-2.85	-0.3	<b>-99.5</b>	100	-4.05	-3.79	4.08	3.89	3.34	<b>99.2</b>
$Y_{\gamma p1}$	<b>-96.4</b>	-11.7	60.5	<b>99.8</b>	88.2	67.4	4.06	<b>99.7</b>	-11.7	88.7	-12.8	67.5	-11.2	4.03	-4.05	100	<b>93</b>	<b>-99.6</b>	<b>-92.6</b>	-79.2	-4.05
$Y_{\gamma p2}$	<b>-90.9</b>	-13.1	51.2	<b>92.8</b>	83.2	63.5	3.8	<b>92.4</b>	-13.4	83.7	-13.9	63.6	-12.5	3.76	-3.79	<b>93</b>	100	<b>-93</b>	-87.3	-74.6	-3.79
$Z_{pp}$	<b>98.3</b>	15.9	-61	<b>-99.6</b>	<b>-90</b>	-68.7	-4.08	<b>-98.9</b>	16.3	<b>-90.5</b>	16.5	-68.7	15.1	-4.04	4.08	<b>-93</b>	100	<b>94.4</b>	<b>94.4</b>	80.7	4.08
$Z_{\pi p}$	<b>96.1</b>	22.9	-57	<b>-92.4</b>	<b>-99.1</b>	-67.1	-3.9	<b>-90.7</b>	24	<b>-99.3</b>	21	-67.1	21.8	-3.83	3.89	<b>-92.6</b>	-87.3	<b>94.4</b>	100	78.8	3.88
$Z_{Kp}$	82	17.8	-48.9	-79	-75.1	<b>-98.2</b>	-3.35	-77.6	18.8	-75.6	17.8	<b>-98.2</b>	14.8	-3.3	3.34	-79.2	-74.6	80.7	78.8	100	3.34
$Z_{\Sigma p}$	4.05	-0.4	-2.57	-4.02	-3.7	-2.84	-1.00	-4.02	-0.332	-3.72	-0.262	-2.85	-0.392	<b>-99.9</b>	<b>99.2</b>	-4.05	-3.79	4.08	3.88	3.34	100

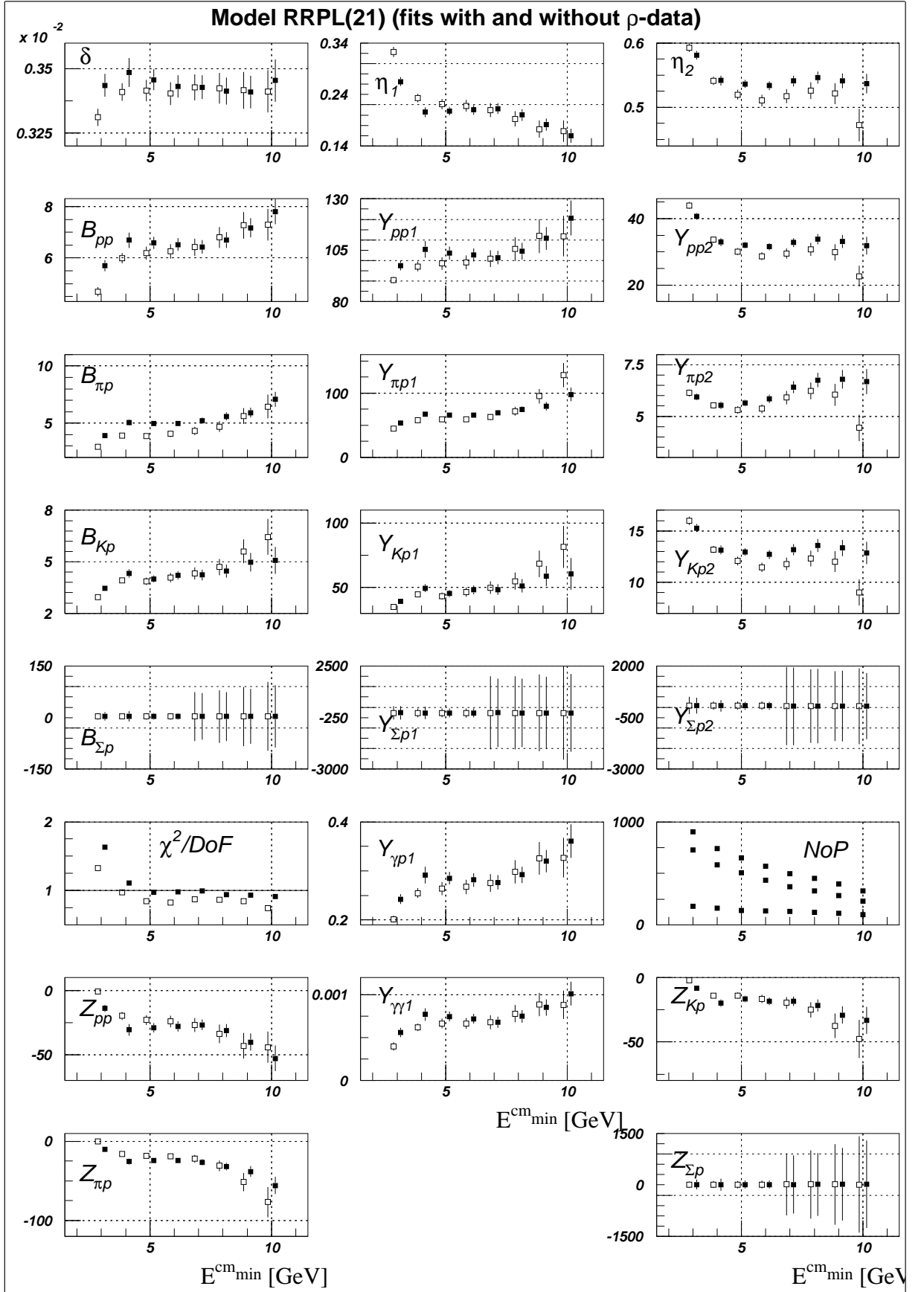


Figure 19: Bold (empty) symbol marks fits with (without)  $\rho$  data and are shifted to the right (left) in energy slightly for the cleareness

